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Experienced Gray Wolf Optimization Through Reinforcement Learning and Neural Networks

E. Emary, Hossam M. Zawbaa, and Crina Grosan

Abstract-In this paper, a variant of gray wolf optimization (GWO) that uses reinforcement learning principles combined with neural networks to enhance the performance is proposed. The aim is to overcome, by reinforced learning, the common challenge of setting the right parameters for the algorithm. In GWO, a single parameter is used to control the exploration/exploitation rate, which influences the performance of the algorithm. Rather than using a global way to change this parameter for all the agents, we use reinforcement learning to set it on an individual basis. The adaptation of the exploration rate for each agent depends on the agent's own experience and the current terrain of the search space. In order to achieve this, experience repository is built based on the neural network to map a set of agents' states to a set of corresponding actions that specifically influence the exploration rate. The experience repository is updated by all the search agents to reflect experience and to enhance the future actions continuously. The resulted algorithm is called experienced GWO (EGWO) and its performance is assessed on solving feature selection problems and on finding optimal weights for neural networks algorithm. We use a set of performance indicators to evaluate the efficiency of the method. Results over various data sets demonstrate an advance of the EGWO over the original GWO and over other metaheuristics, such as genetic algorithms and particle swarm optimization.

Index Terms—Adaptive exploration rate, artificial neural network (ANN), experienced gray wolf optimization (EGWO), gray wolf optimization (GWO), reinforcement learning.

I. INTRODUCTION

COMMON challenge for learning algorithms is the efficient setting of their parameters, which is usually done empirically, after a number of trials. In the majority of cases, a setting of parameters is valid for that particular problem only, and every time the algorithm is applied, a new set of

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parameters has to be initialized. The parameter values are at most suboptimal, as there are never sufficient trials to get the optimal values.

According to [1], learning algorithms suffer from the following.

- The Curse of Dimensionality: Many algorithms need to discretize the state space, which is impossible for control problems with high dimensionality, because the number of discrete states is enormous.
- 2) A Large Number of Learning Trials: Most algorithms need a large number of learning trials, specifically if size of the state space is high, so it is very difficult to apply reinforcement learning to real world tasks.
- 3) *Finding Proper Parameters for the Algorithms:* Many algorithms work well, but only with the right parameter setting. Searching for an appropriate parameter setting is, therefore, crucial, in particular, for time-consuming learning processes. Thus, algorithms which work with fewer parameters or allow a wider range of parameter setting are preferable.
- 4) The Need of a Skilled Learner: Since defining the reward function is not enough, we must also determine a good state-space representation or a proper function approximator, choose an appropriate algorithm and set the parameters of the algorithm. Consequently, additional knowledge and experience are needed when dealing with such learning.

In this paper, we focus on the automatic setting of parameters used by gray wolf optimization (GWO) algorithm, in particular, on the setting of a parameter that plays a significant role in the final result: the exploration/exploitation rate. The metalearner employed for the automatic parameter setting uses reinforcement learning principles [2], [3].

In the conventional reinforcement learning model, an agent is connected to its environment via perception and action. On each step of interaction, the agent receives as input some indications of the current state of the environment and chooses an action that changes the state, and the value of this state transition is reached to the agent through a scalar reinforcement signal [4]. When the search agent chooses an action, it obtains a feedback for that action and uses the feedback to update its data of state-action map. The goal is to determine the actions that tend to increase the long-run sum of values of the reinforcement signal [5].

In order to determine the right set of actions and, in particular, the right action at each time step in GWO, we propose to use neural networks. The input of the neural

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TABLE I Correspondence Between GWO Stages and Space Search

GWO Stage	Interpretation
Prey encircling: adapt wolves posi-	Update solution positions in the
tion in the search space around the	search space around the current op-
prey in any random position	timum
Hunting: adapt wolves positions	Update solution position based
based on the position of alpha,	on the position of the best so-
beta, delta wolves	lutions, considering hierarchically
	three levels
Attack: move to a position between	Update solution position so that it
current position and the prey	gets closer to the current optimum
	by moving towards the optimum
Search: exploration of the search	Exploration of the search space
space by diverging the wolves from	by allowing solution to investigate
each other for more prey so that	new areas in order to find a better
they will converge again for an-	optimum
other attack	

network is the set of all individual action history of all the agents, and the output is the action to be taken by a particular agent. Which means, the action of each agent is individually set in a reinforcement learning manner and a neural network learns it. The methodology is explained in detail in Section III, after a brief introduction of the original GWO algorithm in Section II. The validation of the proposed parameter learning methodology is achieved by considering two optimization problems: feature selection and weight training in neural networks. We perform two types of experiments, one related to feature selection and the other related to multilayer artificial neural networks (ANNs) weights optimization. Experiments on 21 data sets are performed in Section IV for feature selection and on 10 data sets for ANNs weight training and are validated using various metrics and statistical tests. The results indicate a very promising performance of the proposed methodology compared with the manual parameter setting in the original GWO. A similar approach could be either extended to other learning algorithms or, even more complex, generalized to the classes of similar algorithms.

II. PRELIMINARIES

Bioinspired optimization methods are becoming common among researchers due to their simplicity and extensibility. GWO is a relatively new optimization algorithm inspired by the social hierarchy and hunting behavior of the gray wolves in nature [6]. A modified GWO is proposed which employed a good balance between the exploration and exploitation [7]. A multiobjective variant of GWO is developed to optimize the multiobjective problems [8]. A new binary version of GWO is proposed and applied to feature selection problem [9]. In the next subsections (II-A and II-B), we briefly explain the general principles of GWO algorithm and the role of the parameters in the search process.

A. Gray Wolf Optimization

GWO computationally simulates the hunting mechanism of gray wolves. Gray wolves live in a pack with a strict hierarchy: on the top are the *alpha* wolves, responsible for decision making, followed by *beta* and *delta* wolf. The rest of the pack is called *omegas* [6]. Table I shows the corresponding search



Fig. 1. GWO in the search space positioning (adapted from [6]).

and optimization stages of the GWO steps. Naturally, the prey location is the optimal solution and the wolves represent potential solutions in the search space. The wolves closer to the prey are the *alpha* wolves and they are the best solutions so far. Hierarchically, the *beta* wolves are the second best solutions and the *delta* wolves are the third best solutions. Their location in the search space is represented as X_{α} , X_{β} , and X_{δ} . *Omegas* update their position in the search space based on their relative positions from *alpha*, *beta*, and *delta* wolves. Fig. 1 shows the positioning of the wolves and prey and the parameters involved in the search space. For hunting prey, a set of steps are to be applied as follows: prey encircling, hunting, attack, and search again.

1) Prey Encircling: The pack encircles a prey by repositioning individual agents according to the prey location, as follows:

$$\overrightarrow{X}(t+1) = \overrightarrow{X}_{p}(t) + \overrightarrow{A} \cdot \overrightarrow{D}$$
(1)

where t is the iteration, \vec{X}_p is the prey position, \vec{X} is the gray wolf position, the . operator indicates vector entrywise multiplication, and \vec{D} is defined as follows:

$$\overrightarrow{D} = |\overrightarrow{C} \cdot \overrightarrow{X}_{p}(t) - \overrightarrow{X}(t)|$$
(2)

where \overrightarrow{A} and \overrightarrow{C} are coefficient vectors calculated as follows:

$$\overrightarrow{A} = 2a \cdot \overrightarrow{r_1} - a \tag{3}$$

$$\vec{C} = 2\vec{r_2} \tag{4}$$

where *a* is linearly diminished over the course of iterations controlling *exploration* and *exploitation*, and $\overrightarrow{r_1}$ and $\overrightarrow{r_2}$ are random vectors in the range of [0, 1]. The value of *a* is the same for all wolves. These equations indicate that a wolf can update its position in the search space around the prey in any random location.

2) *Hunting:* It is performed by the whole pack based on the information coming from the *alpha*, *beta*, and *delta* wolves, which are expected to know the prey location, as given in the following:

$$\vec{X}(t+1) = \frac{\vec{X}_1 + \vec{X}_2 + \vec{X}_3}{3}$$
 (5)

(6)

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where $\overrightarrow{X_1}$, $\overrightarrow{X_2}$, and $\overrightarrow{X_3}$ are defined as follows:

$$\overrightarrow{X}_1 = |\overrightarrow{X}_a - \overrightarrow{A}_1 \cdot \overrightarrow{D}_a|$$

$$\overrightarrow{X_2} = |\overrightarrow{X_\beta} - \overrightarrow{A_2} \cdot \overrightarrow{D_\beta}| \tag{7}$$

$$\overrightarrow{X}_{3} = |\overrightarrow{X}_{\delta} - \overrightarrow{A}_{3} \cdot \overrightarrow{D}_{\delta}| \tag{8}$$

where $\overrightarrow{X_{\alpha}}$, $\overrightarrow{X_{\beta}}$, and $\overrightarrow{X_{\delta}}$ are the first three best solutions at a given iteration t, $\overrightarrow{A_1}$, $\overrightarrow{A_2}$, and $\overrightarrow{A_3}$ are defined as in (3), and $\overrightarrow{D_{\alpha}}$, $\overrightarrow{D_{\beta}}$, and $\overrightarrow{D_{\delta}}$ are defined using the following:

$$\overrightarrow{D_{\alpha}} = |\overrightarrow{C_1} \cdot \overrightarrow{X_{\alpha}} - \overrightarrow{X}| \tag{9}$$

$$\overrightarrow{D_{\beta}} = |\overrightarrow{C_2} \cdot \overrightarrow{X_{\beta}} - \overrightarrow{X}| \tag{10}$$

$$\overrightarrow{D}_{\delta} = |\overrightarrow{C}_{3} \cdot \overrightarrow{X}_{\delta} - \overrightarrow{X}| \tag{11}$$

where $\overrightarrow{C_1}$, $\overrightarrow{C_2}$, and $\overrightarrow{C_3}$ are defined as in (4).

This is interpreted by the fact that *alpha*, *beta*, and *delta* wolves know the best position of the prey and all the other wolves adapt their positions based on the position of these wolves.

3) Attacking Stage: The agents approach the prey, which is achieved by decrementing the exploration rate *a*. Parameter *a* is linearly updated in each iteration to range from 2 to 0 as follows:

$$a = 2 - t \frac{2}{\text{Max}_{\text{Iter}}}$$
(12)

where *t* is the iteration number and Max_{Iter} is the total number of iterations allowed for the optimization. According to [6], exploration and exploitation are guaranteed by the adaptive values of *a* allowing GWO to transit smoothly between exploration and exploitation, while half of the iterations are dedicated to the exploration and the other half is assigned to exploitation. This stage is interpreted as wolves moving or changing their position to any random position between their current position and the prey position.

4) Search for Prey: Wolves diverge from each other to search for prey. This behavior is modeled by setting large values for parameter a to allow for exploration of the search space. Hence, the wolves diverge from each other to better explore the search space and then converge again to attack when they find a better prey. Any wolf can find a better prey (optimum). If they get closer to the prey, they will become the new *alphas* and the other wolves will be split into *beta*, delta, and omega according to their distance from the prey. Parameter *a* gives random weights to the prey and shows the impact of the prey in characterizing the separation of wolves as in (1) and (2). That helps GWO to demonstrate a more random behavior, favoring exploration and local optima evasion. It is worth mentioning that *a* provides random values at all times keeping in mind the aim to accentuate exploration not only at the beginning of the optimization process but until its end. GWO is described in Algorithm 1.

B. Feed-Forward Artificial Neural Networks

ANNs are a family of models inspired by biological neural networks. They are represented as systems of interconnected neurons that exchange messages between each other. The neural connections have numeric weights that can be tuned

Algorithm 1 GWO

Input: Number of gray wolves (n), maximum iterations (Max_{Iter}) .

Result: The optimal wolf position and its fitness.

- 1) Initialize a population of *n* gray wolves positions randomly.
- Find α, β, and δ as the first three best solutions based on their fitness values.
- 3) t = 0.
 - while $t \leq Max_{Iter}$ do

foreach $Wolf_i \in pack$ **do**

Update current wolf's position according to Eq. (5). end

- Update a, A, and C as in Eqs. (12), (4) and (3).
- Evaluate the positions of individual wolves.

- Update α , β , and δ positions as the first best three solutions in the current population.

$$-t = t + 1.$$

end

4) Select the optimal gray wolf position.

based on experience, making neural nets adaptive to inputs and capable of learning [10]. The primary building block of a neural network is the neuron which has a set of weights. ANN weights are attached to the inputs and an internal nonlinear function maps the input of the neuron to the output given the transfer function as follows:

$$O_i = f\left(w_i^T \cdot x + b_i\right) \tag{13}$$

where O_i is the output of neuron *i*, *f* is the activation function attached to neuron *i*, w_i is a vector of weights attached to neuron *i*, *x* is the input vector of neuron *i*, and b_i is a bias scalar value. Each neural network possesses knowledge that is contained in the connections weights values. Changing the knowledge stored in the network as a function of experience implies a learning rule for modifying the values of the weights. Hence, the most challenging problem in using the ANN models is to choose the appropriate weight bias adaptation method [10]. Usually, the gradient descent method is used to adapt neural network weights based on the following formula:

$$w_{kj}^{t+1} = w_{kj}^t - \eta \frac{\partial E}{\partial w_{kj}}$$
(14)

where w_{kj}^t is the weight linking neuron k to neuron j at time t, and E is suitable error function that computes the deviation between the targeted and the actual output.

According to the availability of training data, neural models can be passive or online. In passive neural models, the neural model is trained using the whole data set at once, while in the case of online models, the data points are not presented as a whole, but it is given one at a time [10].

III. PROPOSED EXPERIENCED GRAY WOLF OPTIMIZATION

Intensification and diversification are the two key components of any metaheuristic algorithm [11]. Intensification

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or exploitation uses the available local information to generate better solutions. Diversification or exploration explores the search space to generate diverse solutions. The balance between exploration and exploitation controls the search behavior of a given optimizer. Excess exploration makes the optimization process to converge quickly, but it may lead to premature convergence. Excess exploitation increases the probability of finding the global optimum, but often slows down the process with a much lower convergence rate. Therefore, resolving the tradeoff between exploration and exploitation is a must to ensure fast global convergence of the optimization process [12]. In almost all modern swarm intelligence optimizers, the exploration rate is adapted throughout the optimization iterations in some predetermined manner to allow for further exploration at some iterations, commonly, at the beginning of the optimization process, and to allow for extra exploitation at some iterations, commonly, at the end of the optimization process. Some optimizers use exploration rate that is linearly inverse proportional to the iteration number. The original GWO linearly decrements the exploration rate as optimization progresses

$$ExpRate = 2 - (t) * (2/T)$$
 (15)

where t is the current iteration, T is the total number of iterations, and ExpRate is the rate of exploration. Although this formula proves efficient for solving numerous optimization problems, it still possesses the following drawbacks.

- 1) *Stagnation:* Once the optimizer approaches the end of the optimization process, it becomes difficult to escape the local optima and find better solutions, because its exploration capability becomes very limited.
- Suboptimal Selection: At the beginning of the optimization process, the optimizer has very high exploration capability, but with this enhanced explorative power, it may leave promising regions to less promising ones.
- 3) *Uniform Behavior:* It is not uncommon to have the same value for the exploration rate for all the search agents, which forces the whole set of wolves to search in the same manner.

The above-mentioned remarks motivate this paper in finding a way to adapt the exploration and to model it individually for each search agent. We proposed to use *experience* as a guide for automatically adjusting the exploration rate. The primary goal is to find a mechanism that maps the different states of search agents to an action set so that the long run goal or fitness function is optimized. To reach such goal and to confront the considerations mentioned earlier regarding such learning, we defined the following components of the system.

A. State-Action Map

The mapping between the states and actions is commonly nonlinear and can be modeled using any nonlinear mapping model, e.g., neural network model. *Incremental* neural networks rather than the *batch* version of the neural network are more adequate, as every time the agent obtains new data, it must use it to update the neural network model.

B. Action Set

For each individual wolf, in order to adapt its exploration rate, we propose a set of actions as follows.

- 1) Increase the Exploration Rate: It takes place as a result of wolf's self-confidence and expertise. This action commonly happens when the wolf finds itself succeeding in some consecutive iterations. The success at a given iteration t is defined by the capability of the search agent to maintain a fitness at time t that is better than its fitness at time t-1. This increases its own confidence and hence increases its exploration rate. Another situation that may motivate such action is that when a successive failure occurs, the agent may need to scout in the search space hoping to find better prey.
- 2) *Decrease Exploration Rate:* Agent's oscillation of fitness may motivate such action and it reflects wrong decision taken by the agent, and hence, it should be cautious in its movements.
- 3) *Keep Exploration Rate:* The current exploration rate is kept static as there is no motivation for neither increase nor decrease it.

The above-mentioned three action will directly affect the exploration rate at the next iteration as follows:

$$\operatorname{ExpRat}_{i}^{t+1} = \begin{cases} \operatorname{ExpRat}_{i}^{t} * (1 + \Delta)(\operatorname{Increase action}) \\ \operatorname{ExpRat}_{i}^{t} * (1 - \Delta)(\operatorname{Decrease action}) \\ \operatorname{ExpRat}_{i}^{t}(\operatorname{Keep action}) \end{cases}$$
(16)

where ExpRat_{i}^{t} is the exploration rate for agent *i* at time *t* and \triangle is the change factor.

C. Agent State

The actions performed change the state of a search agent and the agent is repositioned in the search space and hence acquire a new fitness value. A history of fitnesses of a given agent is used to control its next action so that the agent can accumulate and make use of its past decisions. Formally, the state increases, decreases, or keeps constant the fitness value for a search agent over a time span of T past successive rounds

$$State_{t}^{i} = \left[\dots, sign(f_{t-3}^{i} - f_{t-4}^{i}), sign(f_{t-2}^{i} - f_{t-3}^{i}), \\ sign(f_{t-1}^{i} - f_{t-2}^{i}), sign(f_{t}^{i} - f_{t-1}^{i}) \right]$$
(17)

where State_{t}^{i} is the state vector attached to a given agent *i* at time *t*, $f(t)^{i}$ is the fitness function value for agent *i* at time *t*, and sign(x) is defined as

$$\operatorname{sign}(x) = \begin{cases} 1 & \text{if } x < 0\\ -1 & \text{if } x > 0\\ 0 & \text{otherwise.} \end{cases}$$
(18)

D. Feedback

When an agent leaves a region with good fitness to a region with worse fitness, it receives a negative feedback. On the contrary, when the search agent leaves a bad region to a better one, it receives positive feedback. The agent's own fitness is an indicator of the search region around and decides whether the agent should receive positive or negative feedback. Such feedback can be formulated as

$$\mathsf{Feedback}_{i}^{t} = \begin{cases} +1 & \text{if } f\left(\mathsf{agent}_{i}^{t+1}\right) < f\left(\mathsf{agent}_{i}^{t}\right) \\ -1 & \text{if } f\left(\mathsf{agent}_{i}^{t+1}\right) \ge f\left(\mathsf{agent}_{i}^{t}\right) \end{cases}$$
(19)

where Feedback^t_i is the feedback for agent *i* at time *t*, and $f(agent^t_i)$ is the fitness of agent *i* at time *t*.

Models that map situations to actions to maximize some reward functions are commonly called reinforcement learning models [13]. In such models, the learner is not told which actions to take but instead discovers which actions yield to higher reward by trying them [2]. Two distinguishing features are commonly used to identify such models: 1) trial-anderror search and 2) delayed reward. According to our problem formulation, we consider a set of actions, state, feedback, and the state-action mapping model. The state action mapping model is a neural network with a single hidden layer. ANNs are commonly used to map an unknown (generally nonlinear) function and have well-established training methods [10]. The set of previously mentioned actions increase, decrease, and keep exploration rate are encoded into neural network nodes in the output layer. Therefore, the network has three nodes in the output layer corresponding to the three applicable actions, with 1 on the node indicating the action that will be applied and a 0 value on the other two nodes. The state vector described in (17) with length T is used as input to the neural model. So, the number of nodes in the input layer is exactly T nodes. The hidden layer has a 2 * T + 1 nodes [10].

Common to reinforcement learning, the feedback signal, computed as in (19), is used to adapt the experience of the model through training. The neural weights are adapted according to the action taken and the feedback received at time *t*. The weights of the neural model are adapted by *rewarding* or *punishing* the winning node. The winning node, representing the applied action, is rewarded by moving its current output to be closer to 1 in the case of receiving *positive* feedback through adapting its attached weights [14]. In the case of receiving *negative* feedback, the node attached to the applied action is *punished* by moving its output to be closer to 0 through updating its assigned weights. Equation (20) employs the gradient descent method to adapt the weights of the output layer attached to the winning node given a target value of 1 or 0 in the case of positive or negative feedback

$$w_i^{t+1} = w_i^t + \eta x (d_i - y_i) y_i (1 - y_i)$$
(20)

where w_i^t is the weight for output node *i* at time *t*, *x* is the input state, y_i is the actual output on node *i*, and d_i is the desired output on node *i* which is set either to 1 when receiving positive feedback or 0 when receiving negative feedback. The update is propagated to the hidden weights as follows:

$$w_i^{t+1} = w_i^t + \eta x y_j (1 - y_j) \sum_{i}^{o} w_{ij} ((d_i - y_i) y_i (1 - y_i)) \quad (21)$$

where η is the learning rate, *o* is the number of actions, y_j is the output of the hidden node *j*, y_i is the output of node *i*, and *x* is the input state. The wining node/action selection can



Fig. 2. Number of punishments and rewards received by all the agents during the optimization.



Fig. 3. Flow chart describing the state change of ANN actions.

be formulated as follows:

Winner =
$$\min_{i=1}^{3} |1 - o_i|$$
 (22)

where o_i is the value of the output node *i*.

The main assumption to propose such a training model is that the state-action mapping applies a static unknown function to be estimated in a trial and error manner, but if such mapping is not static or changes slightly, the system tends to take random actions and no experience is acquired. Such a training manner is very natural when the trainability is lost in case of fast changing environment [15]. Fig. 2 shows the total number of punishments and rewards acquired by all search agents during the optimization process. We can remark from Fig. 2 that as optimization progresses, the experience of the search agents is enhanced, and hence, the number of correct actions (rewards) increases, while the number of wrong actions (punishments) decreases. This proves the capability of the proposed strategy to converge to optimal state-action map and, hence, to optimally timed parameters. The proposed algorithm is called EGWO, and is formally given in Algorithm 2. Fig. 3 outlines the flow of state change as a response to actions produced by the neural network.

IV. EXPERIMENTAL RESULTS AND DISCUSSION

This section summarizes the results from applying the proposed experienced GWO on two main applications, namely, *feature selection* and *neural network weight adaptation*. The next two subsections (IV-A and IV-B) contain the results and the analysis for each application. We use a set of qualitative

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Algorithm 2 EGWO

Input: Number of gray wolves (*n*), maximum iterations (Max_{Iter}) , state vector (*T*), exploration change factor \triangle . **Result**: The optimal wolf position and its fitness.

- 1) Randomly initialize a population of n wolves.
- 2) Initialize a set of n values a_i representing the exploration rate attached to each wolf.
- 3) Find α , β , and δ solutions based on fitness values.
- 4) Initialize the state-action neural network to random values.
- 5) t = 0.

while $t \leq Max_{Iter}$ do

foreach $Wolf_i \in pack$ **do**

- Update wolf's current position according to Eq. (5).
- Calculate the $Feedback_i^t$ according to Eq. 19.
- Update the state-action neural network given

Action_{t-1}, state_{t-1} and Feedback_t according to Eqs. (20) and (21).

- Update $Wolf_i$ state vector according to Eq. (17).

- Update the exploration parameter a_i attached to $Wolf_i$ as in Eq. (16).

end

- Update A and C as in Eqs. (3) and (4).
- Evaluate the positions of individual wolves.
- Update α , β , and δ positions as the first best three solutions in the current population.
- -t = t + 1.
- end
- 6) Select the optimal gray wolf position.

measures in order to analyze the results obtained by the methods we apply. The first three metrics give a measure of the mean, best, and worst expected performance of the algorithms. The fourth measure is adopted to show the ability of the optimizer to converge to the same optimal solution. The fifth and sixth metrics show the accuracy of the classification. The seventh and eighth metrics are a measure of the size of the selected features set (we expect a low number of features and a high accuracy). The last three metrics are used for directly comparing two algorithms and show whether the difference between them is significant or not.

- 1) *Mean Fitness:* It is an average value of all the solutions in the final sets obtained by an optimizer in a number of individual runs [16].
- Best Fitness: It is the best solution found by an optimizer in all the final sets resulted from a number of individual runs [16].
- 3) *Worst Fitness:* It is the worst solution found by an optimizer in all the final sets resulted from a number of individual runs [16].
- 4) *Standard Deviation:* It is used to ensure that the optimizer convergences to the same optimal and ensures repeatability of the results. It is computed over all the sets of final solutions obtained by an optimizer in a number of individual runs [17].

- Classifier Mean Square Error (CMSE): It is a measure of classifier's average performance on the test data. It is averaged over all final sets in all the independent runs [18].
- 6) *Root-Mean-Square Error (RMSE):* It measures the root average squared error of the difference between actual output and the predicted one. It is averaged over all final sets in all the independent runs [18].
- Average Selected Feature: It represents the average size of the selected features subset. The average is computed for each final set of solutions in multiple individual runs.
- 8) Average Fisher Score: It evaluates a feature subset such that in the data space spanned by the selected features, the distances between data points in different classes are as large as possible, while the distances between data points in the same class are as small as possible [19]. Fisher score in this paper is calculated for individual features given the class labels; as follows:

$$F_j = \frac{\sum_{k=1}^{c} n_k \left(\mu_k^j - \mu^j\right)^2}{(\sigma^j)^2}$$
(23)

where F_j is the Fisher index for feature j, μ^j and $(\sigma^j)^2$ are the mean and standard deviation (std) of the whole data set, n_k is the size of class k, and μ_k^j is the mean of class k. The Fisher for a set of features is defined as

$$F_{\text{tot}} = \frac{1}{S} \sum_{i=1}^{S} F_i \tag{24}$$

where S is the number of selected features. The average Fisher score over a set of N runs is defined as

Fishr-score =
$$\frac{1}{N} \sum_{i=1}^{N} F_{\text{tot}}^{i}$$
 (25)

where F_{tot}^{i} is the Fisher score computed for selected feature set on run *i*.

9) Wilcoxon Rank Sum Test: It is a nonparametric test for significance assessment. The test assigns rank to all the scores considered as one group and, then, sums the ranks of each group [20]. The test statistic relays on calculating W as follows:

$$W = \sum_{i=1}^{N} \operatorname{sgn}(x_{2,i} - x_{1,i}).R_i)$$
(26)

where $x_{2,i}$ and $x_{1,i}$ are the best fitness obtained from the first and second optimizers on run *i*, R_i is the rank of difference between $x_{2,i}$ and $x_{1,i}$, and sgn(x) is the standard sign function.

10) *T-Test:* It measures the statistical significance and decides whether or not the difference between the average values of two sample groups reflects the real difference in the population (set) the groups were sampled from [21], as follows:

$$t = \frac{\bar{x} - \mu_0}{\frac{S}{\sqrt{n}}} \tag{27}$$

where μ_0 is the mean of the t-distribution and (S/\sqrt{n}) is its std.

11) *Average Run Time:* It is the time (in seconds) required by an optimization algorithm for a number of different runs.

A. EGWO Applied for Feature Selection

Finding a feature combination that maximizes a given classifier performance is a challenging problem. A data set with k features has 2^k different possible choices. The wrapper-based method for feature selection is a very common and reasonably efficient approach, but it comes with a huge processing cost as the classifier must be evaluated at each selected feature combination [22]. The main characteristic of the wrapper-based method is the use of the classifier as a guide to feature selection procedure [23]. The *classifier* adopted in this paper is the *K*-nearest neighbor (KNN) [24]. KNN is a supervised learning algorithm that classifies an unknown sample instance based on the majority of the KNN category. According to the direct formulation of wrapper-based approach for feature selection, the *evaluation criteria* (the fitness to optimize) is formulated as

$$\operatorname{Fitness}(D) = \alpha E_M(D) + \beta \frac{|M|}{|N|}$$
(28)

where $E_M(D)$ is the error rate for the classifier of condition feature set D, M is the size of selected feature subset, and N is the total number of features. $\alpha \in [0, 1]$ and $\beta = 1 - \alpha$ are constants which control the importance of classification accuracy and feature reduction. Any possible combination of features D can be evaluated, and hence, this function is continuously defined on the whole feature space with each component of the vector D in the range [0, 1] and such fitness function is generally nondifferentiable.

The *search methods* employed in this paper are the proposed EGWO, GWO, particle swarm optimization (PSO) [25], and genetic algorithms (GAs) [26].

1) Initialization: Four initialization methods are adopted in this paper differing from one another with respect to the following aspects.

- 1) *Population Diversity:* The ability of an optimizer to produce variants of the given initial population is a valuable property.
- Closeness to Expected Optimal Solution: The capability to efficiently search the space for the optimal solution is must for a successful optimizer. Hence, it is intended to force the initial search agents to be apart from or close to the expected optimal solution.
- Resemblance to Forward and Backward Selection: Each of these has its own strengths and weaknesses, and hence, we would like to assess the initialization impact on the feature selection process.

Fig. 4 shows the initial wolves positions using the four initialization methods and the details about these techniques are as follows.

a) Small initialization: Search agents are initialized with a small number of randomly selected features. Therefore, if

		3	ma	II			Mixed
$ \begin{bmatrix} 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{bmatrix} $	$ \begin{array}{c} 1 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ $	$ \begin{array}{c} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \\ 0 \end{array} $	0 0 0 0 0 1	$ \begin{array}{c} 0 \\ 0 \\ 0 \\ 1 \\ 0 \end{array} $	$ \begin{array}{c} 0 \\ 0 \\ 1 \\ 0 \\ 0 \\ 0 \end{array} $	$ \begin{bmatrix} 0 \\ 0 \\ 0 \\ 1 \\ 0 \\ 1 \end{bmatrix} $	$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 1 & 1 \\ 0 & 1 & 0 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 0 & 0 & 1 & 1 \\ 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 & 0 & 1 & 1 \end{bmatrix}$
		Ur	nifo	rm			MRMR
$\begin{bmatrix} 0\\1\\0\\1\\0 \end{bmatrix}$	$egin{array}{c} 0 \\ 1 \\ 0 \\ 1 \\ 0 \end{array}$	$egin{array}{c} 1 \\ 0 \\ 1 \\ 1 \\ 0 \end{array}$	$ \begin{array}{c} 0 \\ 0 \\ 1 \\ 0 \end{array} $	$egin{array}{c} 1 \\ 0 \\ 0 \\ 1 \\ 1 \end{array}$	$ \begin{array}{c} 1 \\ 0 \\ 0 \\ 1 \\ 0 \end{array} $	$ 1 \\ 0 \\ 1 \\ 1 \\ 0 0 $	$\begin{bmatrix} 0.8 & 0 & 0 & 1 & 0 & 0 & 1 \\ 0.1 & 1 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 0 & 0 & 1 & 0 \\ 0.1 & 0 & 1 & 1 & 1 & 0 & 0 \\ 0 & 1 & 1 & 0 & 1 & 1 & 0 \end{bmatrix}$

Fig. 4. Sample initial wolves positions using different initializations with nine search agents and six dimensions.

the number of agents is less than the number of features, we will see that each search agent will have a single dimension with value 1. Of course, the optimizer will search for feature(s) to be set to 1 to enhance the fitness function value as in the standard forward selection of features. This method is expected to test the *global search* ability of an optimizer as the initial search agents' positions are commonly away from the expected optimum. Therefore, the optimizer has to use global search operators to derive better solutions.

b) Mixed initialization: Half of the search agents are initialized using the small initialization and the other half are initialized using the large initialization method with more random features. Some search agents are close to the expected optimal solution and the other search agents are away from it. Hence, it provides much more *diversity* of the population as the search agents are expected to be far from each other. This method takes both the merits of small and large initialization [23].

c) Uniform initialization: Each feature has the same probability of being selected. This method is the most common initialization where the agents are randomly placed in the search space.

d) MRMR initialization: The minimum redundancy maximum relevance (MRMR) combines two criteria for feature selection [27], namely, *relevance* with the target class and *redundancy* to other features. In order to define MRMR, we will use the mutual dependence between two random variables *X* and *Y* given as

$$I(X;Y) = \sum_{x \in X} \sum_{y \in Y} p(x;y) \log \frac{p(x;y)}{p(x)p(y)}$$
(29)

where p(x; y) is joint probability distribution of x and Y, and p(x) and p(y) are the marginal probability distribution functions of X and Y.

For our feature selection problem, let F_i and F_j be two features from the set F of N features and c the class label. 8

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The *maximum relevance* method selects the top M best features based on their mutual dependence with class c

$$\max_{F} \frac{1}{N} \sum_{F_i \in F} I(F_i; c).$$
(30)

These top M features may not be the best M features as there might be correlations among them. Thus, the redundancy is removed using the *minimum redundancy* criterion

$$\min_{F} \frac{1}{N^2} \sum_{F_i, F_j \in F} I(F_i; F_j).$$
(31)

The *MRMR* initialization combines both these objectives. Iteratively, if M - 1 features are selected in the set S_{M-1} , the *M*th feature is selected by maximizing the single variable relevance minus redundancy

$$\max_{F_i \in F - S_{M-1}} \left(I(F_i; c) - \frac{1}{M-1} \sum_{F_j \in S_{M-1}} I(F_i; F_j) \right). \quad (32)$$

Using the concept of mutual information, the MRMR method selects variables that have the *highest relevance* with the target class and *minimally redundant* as well, i.e., dissimilar to each other. MRMR is normalized along the feature set as

$$P_i^d = \frac{\text{MRMR}_i}{\max_{i=1}^d \text{MRMR}_i}$$
(33)

where P_i is the search agent position in dimension d, MRMR_{*i*} is the MRMR value for feature *i*, and *d* is the problem dimension.

MRMR is used to initialize one search agent and the rest of search agents are set at random positions in the search space.

2) Data Sets: The 21 data sets in Table II from the UCI machine learning repository [28] are used for tests and comparisons. The data sets are selected to ensure a large variety regarding the number of features and the number of instances. Each data set is divided randomly into three different equal parts for *validation*, *training*, and *testing* using cross validation. Each experiment with each algorithm repeated 30 times to ensure the stability and the statistical significance of the results.

3) Parameter Settings: The global and optimizer-specific parameter settings are outlined in Table III. All the parameters are set either according to domain-specific knowledge as the α and β parameters of the fitness function, or based on a trial and error methodology on small simulations or from previous experiments reported in the literature in the case of the rest parameters.

4) Results and Discussion: Fig. 5(a) shows the statistical indicators computed for GWO, EGWO, PSO, and GA using the uniform initialization method. We can observe that the performance of EGWO is superior to that of GWO in the average performance. We can also see that the std of EGWO is comparable to that of GWO, which ensures repeatability of results and convergence to the same optimum. The enhanced performance of EGWO is due to the fact that the search agents learn the ill-promising regions of the search space and jump out of these regions to more promising regions.

TABLE II DATA SETS DESCRIPTION

Data No.	Dataset	No. Features	No. instances
1	Breastcancer	9	699
2	BreastEW	30	569
3	Clean1	166	476
4	Clean2	166	6598
5	CongressEW	16	435
6	Exactly	13	1000
7	Exactly2	13	1000
8	HeartEW	13	270
9	IonosphereEW	34	351
10	KrvskpEW	36	3196
11	Lymphography	18	148
12	M-of-n	13	1000
13	PenglungEW	325	073
14	Semeion	265	1593
15	SonarEW	60	208
16	SpectEW	22	267
17	Tic-tac-toe	9	958
18	Vote	16	300
19	WaveformEW	40	5000
20	WineEW	13	178
21	Zoo	16	101

TABLE III PARAMETER SETTINGS FOR EXPERIMENTS

Parameter	Value(s)
No of search agents	8
No of iterations	70
Problem dimension	Number of features
Search domain	[0 1]
No. runs of each optimizer	30
α in the fitness function	0.99
β in the fitness function	0.01
Δ for changing the exploration rate	0.1
n learning rate for neural network	0.2
T the length of state vector	5
Crossover Fraction in GA	0.8
Inertia factor of PSO	0.1
Individual-best acceleration factor of PSO	0.1

That is possible at all stages, not only at the beginning of search process due to the way in which the exploration rate parameter a_i is controlled. Since every search agent has its own exploration parameter, the diversity of behavior is assured and hence tolerates for stagnation particularly in the end stages of optimization. Individual agents in the EGWO swarm can still increase the exploration rate even in the latter stages of the optimization process, allowing for escaping local minima and premature convergence. In the standard GWO, the exploration rate is linearly decreased during the search process, allowing for a large exploration at the beginning and more local search toward the end. The same conclusion can be derived from the results obtained using the small, mix, and MRMR initialization methods in Fig. 5(b)–(d), respectively, when EGWO performs better in average than the other methods. Small initialization forces the search agents to be initialized away from the expected optimal solution and the agents are forced to keep diversity. Hence, it adds difficulty to the optimizer to escape from such situation. EGWO has an advantage again here as it adapts its exploration rate based on (what has learned from) experience rather than using a formula that does it iteratively and ignoring previous performance and can quickly adapt its

TABLE IV
AVERAGE CMSE, SELECTED FEATURE, AND FISHER SCORE USING UNIFORM INITIALIZATION

		CMS	SE		Selected feature				Fisher score			
Data No.	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA
1	0.040	0.040	0.046	0.037	0.457	0.442	0.443	0.439	0.685	0.676	0.590	0.651
2	0.058	0.068	0.065	0.067	0.326	0.344	0.340	0.352	0.255	0.210	0.214	0.242
3	0.226	0.240	0.249	0.239	0.235	0.281	0.283	0.293	0.085	0.006	0.075	0.046
4	0.045	0.046	0.042	0.048	0.278	0.345	0.349	0.363	0.005	0.005	0.005	0.046
5	0.060	0.062	0.053	0.069	0.201	0.222	0.222	0.225	0.160	0.161	0.189	0.122
6	0.302	0.264	0.264	0.268	0.376	0.470	0.476	0.475	0.001	0.001	0.014	0.001
7	0.253	0.243	0.238	0.250	0.239	0.137	0.145	0.129	0.061	0.001	0.069	0.057
8	0.236	0.233	0.226	0.236	0.470	0.427	0.429	0.426	0.088	0.081	0.010	0.100
9	0.151	0.155	0.153	0.155	0.222	0.240	0.241	0.246	0.048	0.020	0.041	0.029
10	0.054	0.087	0.090	0.092	0.281	0.324	0.330	0.321	0.018	0.018	0.012	0.010
11	0.272	0.273	0.275	0.276	0.272	0.272	0.273	0.277	0.120	0.088	0.107	0.011
12	0.064	0.068	0.065	0.077	0.427	0.479	0.474	0.489	0.027	0.029	0.026	0.006
13	0.294	0.327	0.331	0.336	0.157	0.188	0.194	0.181	0.121	0.143	0.108	0.117
14	0.042	0.043	0.048	0.047	0.232	0.288	0.290	0.291	0.006	0.006	0.005	0.003
15	0.312	0.298	0.298	0.298	0.289	0.276	0.284	0.273	0.024	0.013	0.003	0.015
16	0.193	0.203	0.197	0.196	0.293	0.237	0.237	0.256	0.018	0.016	0.016	0.017
17	0.255	0.255	0.258	0.263	0.580	0.617	0.625	0.626	0.059	0.050	0.057	0.024
18	0.070	0.081	0.083	0.071	0.208	0.229	0.234	0.235	0.140	0.136	0.092	0.157
19	0.208	0.220	0.218	0.221	0.367	0.386	0.389	0.389	0.218	0.120	0.201	0.068
20	0.065	0.062	0.060	0.067	0.342	0.373	0.381	0.392	0.474	0.461	0.454	0.428
21	0.158	0.153	0.143	0.159	0.292	0.322	0.328	0.334	12.576	11.377	11.282	11.294



Fig. 5. Box-plot of fitness values for the different initializations. (a) Uniform initialization. (b) Small initialization. (c) Mix initialization. (d) MRMR initialization.

exploration rate to approach the global optima while leaving the nonpromising regions. Fig. 6 outlines the snapshot of the exploration rates for five agents where we can see the difference in such rate between the different agents which motivates the global fitness function to reach the optimum.

When using a *mixed initialization*, all optimizers perform better than using *small initialization* and *uniform initialization* which can be interpreted by the variability of the initial position in the search space, some search agents being initialized close to the expected optimal solution. We can remark that the EGWO still performs better. Fig. 7 shows the behavior of a single search agent where we can see that the search agent adapts its own exploration in response to its own fitness and such behavior allows the search agent to keep its exploration capability even at the end stages of the optimization, trying to find better promising regions.



Fig. 6. Five agents with their exploration rates and the global fitness value.



Fig. 7. Single agent with its exploration rate, its fitness, and the global fitness.

We can observe very good results using the MRMR initialization for all the algorithms. The good performance can be explained by the fact that the initial population already contains a nearly optimal solution and the optimizer is required only to enhance such solution. All these methods include a mechanism by which the solutions in the swarm tend to follow the best solution found so far. But, there are still situations in which the nearly optimal solution can be far away from the global optimum, requiring again very good explorations

		CMS	SE			Selected 1	feature		Fisher score			
Data No.	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA
1	0.065	0.066	0.066	0.077	0.250	0.259	0.251	0.266	0.384	0.368	0.360	0.347
2	0.152	0.164	0.175	0.155	0.031	0.044	0.035	0.033	0.134	0.127	0.140	0.115
3	0.385	0.383	0.386	0.379	0.009	0.010	0.016	0.013	0.750	0.740	0.400	0.011
4	0.106	0.106	0.109	0.109	0.016	0.013	0.024	0.012	0.009	0.006	0.014	0.015
5	0.129	0.142	0.140	0.141	0.118	0.111	0.105	0.125	0.064	0.061	0.048	0.062
6	0.312	0.312	0.311	0.287	0.077	0.077	0.087	0.080	0.002	0.002	0.022	0.002
7	0.242	0.242	0.243	0.246	0.077	0.077	0.075	0.072	0.009	0.008	0.008	0.001
8	0.307	0.280	0.252	0.284	0.128	0.171	0.171	0.169	0.023	0.028	0.029	0.016
9	0.227	0.236	0.232	0.244	0.052	0.056	0.059	0.061	0.006	0.007	0.019	0.002
10	0.445	0.418	0.408	0.405	0.043	0.040	0.054	0.054	0.001	0.001	0.009	0.001
11	0.388	0.365	0.378	0.357	0.080	0.080	0.103	0.075	0.068	0.018	0.030	0.020
12	0.310	0.315	0.333	0.316	0.128	0.103	0.107	0.087	0.005	0.006	0.010	0.001
13	0.535	0.527	0.533	0.521	0.006	0.005	0.014	0.003	0.004	0.005	0.003	0.005
14	0.099	0.099	0.084	0.107	0.004	0.004	0.007	0.015	0.004	0.005	0.002	0.001
15	0.384	0.351	0.368	0.360	0.020	0.030	0.024	0.037	0.002	0.002	0.014	0.005
16	0.206	0.223	0.215	0.205	0.051	0.051	0.035	0.049	0.003	0.003	0.002	0.006
17	0.323	0.334	0.361	0.338	0.185	0.160	0.172	0.178	0.003	0.002	0.023	0.009
18	0.152	0.124	0.136	0.132	0.104	0.104	0.098	0.098	0.076	0.060	0.072	0.055
19	0.502	0.508	0.505	0.507	0.039	0.039	0.046	0.042	0.011	0.009	0.009	0.024

 TABLE V

 Average CMSE, Selected Feature, and Fisher Score Using Small Initialization

TABLE VI Average CMSE, Selected Feature, and Fisher Score Using Mixed Initialization

0.179

0.118

0.174

0.125

0.170

0.110

0.282

3.818

0.265

3.044

0.270

3.065

0.265

3.041

0.165

0.110

		CMS	SE			Selected f	feature			Fisher	score	
Data No.	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA
1	0.042	0.042	0.039	0.036	0.457	0.543	0.544	0.549	0.681	0.746	0.742	0.751
2	0.063	0.060	0.059	0.047	0.330	0.333	0.324	0.339	0.194	0.207	0.202	0.226
3	0.212	0.235	0.242	0.234	0.246	0.255	0.248	0.257	0.005	0.005	0.007	0.01
4	0.046	0.046	0.055	0.064	0.355	0.414	0.407	0.394	0.006	0.007	0.011	0.028
5	0.071	0.055	0.072	0.070	0.250	0.222	0.224	0.226	0.167	0.158	0.153	0.155
6	0.281	0.262	0.297	0.299	0.513	0.547	0.564	0.554	0.001	0.001	0.008	0.004
7	0.250	0.256	0.261	0.263	0.436	0.436	0.433	0.428	0.001	0.001	0.004	0.009
8	0.237	0.207	0.204	0.210	0.453	0.513	0.514	0.513	0.077	0.089	0.080	0.117
9	0.144	0.149	0.140	0.151	0.222	0.258	0.264	0.254	0.033	0.022	0.025	0.031
10	0.048	0.039	0.051	0.027	0.358	0.407	0.406	0.424	0.020	0.020	0.007	0.025
11	0.275	0.282	0.282	0.283	0.284	0.370	0.363	0.370	0.110	0.101	0.086	0.114
12	0.017	0.040	0.041	0.050	0.462	0.504	0.516	0.506	0.038	0.031	0.037	0.031
13	0.282	0.323	0.320	0.322	0.142	0.175	0.177	0.165	0.144	0.135	0.128	0.137
14	0.042	0.038	0.046	0.032	0.284	0.350	0.357	0.343	0.026	0.008	0.022	0.012
15	0.281	0.282	0.297	0.282	0.265	0.302	0.310	0.288	0.042	0.016	0.015	0.031
16	0.200	0.211	0.208	0.213	0.247	0.379	0.399	0.386	0.045	0.021	0.022	0.033
17	0.253	0.259	0.267	0.269	0.679	0.753	0.773	0.759	0.010	0.006	0.009	0.004
18	0.070	0.071	0.081	0.082	0.208	0.181	0.165	0.173	0.138	0.126	0.134	0.133
19	0.218	0.224	0.215	0.216	0.533	0.544	0.543	0.573	0.141	0.135	0.118	0.123
20	0.080	0.080	0.092	0.092	0.359	0.376	0.356	0.485	0.462	0.450	0.480	0.446
21	0.114	0.125	0.119	0.137	0.292	0.319	0.302	0.323	15.528	14.580	14.565	14.593

of the search space. This is why the exploration ability of EGWO brings it again in advantage compared with the other methods, not only regarding the accuracy of the convergence but also the size of the selected features, EGWO being able to detect the smallest number of relevant features for most of the test cases.

Tables IV–VII show the performance on the test data in terms of classification accuracy, the average size of the selected features set, and the average Fisher score. For the uniform initialization where the initial population is very random, EGWO still obtains the smallest features set for about 77% of the data sets, with the best classification accuracy for 72% of the data sets and the best Fisher score for over 66% of the data while for the remaining data sets still obtains very good results.

For the small initialization, EGWO still dominates the other methods in over 50% of the data sets. Results are better in the case of mixed initialization and MRMR initialization. EGWO obtains the smallest number of features for over 76% of the data sets, the best accuracy for over 57% of the data sets, and the best Fisher score for over 50% of the tests.

Regarding the running time (results in Table VIII), EGWO and GWO perform slower than PSO and GA for the majority of the data sets, but the difference is not really high in all the cases. The extra time is consumed in the continual training of the neural network model and the retrieval of action decision. Such increase in time consumption in comparison to enhanced optimization seems to be tolerable in many applications. This could be possibly improved by applying only reinforcement

20

21

0.242

0.346

0.148

0.408

0.154

0.410

0.136

0.412

	TABLE VII	
AVERAGE CMSE,	SELECTED FEATURE, SIZE AND FISHER SCORE USING MRMR I	NITIALIZATION

		CMS	SE			Selection	1 Size			Fisher	score	
Data No.	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA
1	0.042	0.042	0.039	0.036	0.457	0.543	0.544	0.549	0.681	0.746	0.742	0.751
2	0.063	0.060	0.059	0.047	0.330	0.333	0.324	0.339	0.194	0.207	0.202	0.226
3	0.212	0.235	0.242	0.234	0.246	0.255	0.248	0.257	0.007	0.005	0.007	0.001
4	0.046	0.046	0.055	0.064	0.355	0.414	0.407	0.394	0.006	0.007	0.011	0.028
5	0.071	0.055	0.072	0.070	0.250	0.222	0.224	0.226	0.167	0.158	0.153	0.155
6	0.281	0.262	0.297	0.299	0.513	0.547	0.564	0.554	0.001	0.001	0.008	0.004
7	0.250	0.256	0.261	0.263	0.436	0.436	0.433	0.428	0.001	0.001	0.004	0.009
8	0.237	0.207	0.204	0.210	0.453	0.513	0.514	0.513	0.097	0.089	0.080	0.117
9	0.144	0.149	0.140	0.151	0.222	0.258	0.264	0.254	0.033	0.02	0.025	0.031
10	0.048	0.039	0.051	0.027	0.358	0.407	0.406	0.424	0.026	0.020	0.007	0.025
11	0.275	0.282	0.282	0.283	0.284	0.370	0.363	0.370	0.110	0.101	0.086	0.114
12	0.017	0.040	0.041	0.050	0.462	0.504	0.516	0.506	0.031	0.031	0.037	0.031
13	0.282	0.323	0.320	0.322	0.142	0.175	0.177	0.165	0.144	0.135	0.128	0.137
14	0.042	0.038	0.046	0.032	0.284	0.350	0.357	0.343	0.006	0.008	0.022	0.012
15	0.281	0.282	0.297	0.282	0.265	0.302	0.310	0.288	0.042	0.016	0.015	0.031
16	0.200	0.211	0.208	0.213	0.247	0.379	0.399	0.386	0.045	0.021	0.022	0.033
17	0.253	0.259	0.267	0.269	0.679	0.753	0.773	0.759	0.010	0.006	0.009	0.004
18	0.070	0.071	0.081	0.082	0.208	0.181	0.165	0.173	0.138	0.126	0.134	0.133
19	0.218	0.224	0.215	0.216	0.533	0.544	0.543	0.573	0.141	0.135	0.118	0.123
20	0.080	0.080	0.092	0.092	0.359	0.376	0.356	0.385	0.462	0.450	0.480	0.446
21	0.114	0.125	0.119	0.137	0.292	0.319	0.302	0.323	12.528	14.580	14.565	14.593

TABLE VIII Average Running Time in Seconds for All Initialization Methods

Data No.	EGWO	GWO	PSO	GA
1	11.521	11.394	14.228	9.541
2	12.322	11.844	9.554	7.014
3	44.652	44.737	44.021	42.424
4	1100.702	1076.420	1075.793	1076.158
5	9.640	9.670	9.744	4.540
6	14.699	13.413	13.498	13.342
7	14.063	13.016	13.438	12.143
8	8.871	8.798	8.083	4.524
9	10.094	10.032	12.053	8.601
10	79.255	80.230	83.375	84.586
11	8.826	8.367	5.460	11.342
12	14.784	15.245	15.906	12.387
13	54.400	54.147	49.889	53.090
14	134.523	130.479	133.261	133.105
15	9.950	9.705	11.493	10.903
16	9.097	8.877	13.155	8.105
17	14.385	14.142	18.379	13.480
18	8.795	8.611	5.514	13.762
19	220.967	210.184	209.562	213.813
20	8.927	8.669	4.632	14.005
21	9.083	8.875	4.864	8.657

learning at quantized optimization steps. Regarding the added storage cost for the proposed algorithm, the ANN weights could be stored and the short history per wolf could also be kept. The neural model in the current implementation is stored as two matrices with sizes $T \times (2T + 1)$ and $(2T + 1) \times 3$. The wolf's short history is a vector of length T.

Significance tests have the role of comparing two optimizers in order to find a statistically significant difference between them. Table IX shows the results of T-test and Wilcoxon's test calculated on the different initialization methods for all the four optimizers. We are interested in the performance of EGWO against the other algorithms; thus, we report all the comparisons with EGWO only. EGWO performs better than GWO, PSO, and GA as per T-test results at a significance

TABLE IX WILCOXON AND T-TEST FOR ALL INITIALIZATION METHODS

Initializer	Optimizer_1	Optimizer_2	Wilcoxon	T-test
Uniform	GWO	EGWO	0.100	0.049
Uniform	PSO	EGWO	0.050	0.040
Uniform	GA	EGWO	0.049	0.042
Small	GWO	EGWO	0.082	0.052
Small	PSO	EGWO	0.05	0.05
Small	GA	EGWO	0.047	0.048
Mixed	GWO	EGWO	0.100	0.097
Mixed	PSO	EGWO	0.049	0.07
Mixed	GA	EGWO	0.048	0.05
MRMR	GWO	EGWO	0.077	0.030
MRMR	PSO	EGWO	0.048	0.037
MRMR	GA	EGWO	0.049	0.034

TABLE X DATA SET USED FOR REGRESSION

Data No.	Dataset	No. Features	No. instances
1	CASP	9	45730
2	CBM	17	11934
3	ССРР	4	47840
4	ENB2012_Y1	8	768
5	ENB2012_Y2	8	768
6	Housing	13	506
7	Relation Network	22	53413
8	Slump_test	10	103
9	Yacht_hydrodynamics	6	308
10	forest Fire	12	517

level of 5% when using the uniform and MRMR methods, while less importance value is observed when using the small and mixed initializations. This confirms that the learning of the adaptation rate in EGWO really helps the optimization process, regardless of the initial position of the agents, whether close to an optimum or random over the search space. We can also observe that the proposed EGWO has significant advance over PSO and GA using Wilcoxon and T-test at a significance level of 5% regardless of the used initialization method.

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	Mean fitness				Best fitness				Worst fitness			
Data No.	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA
1	28.250	28.064	28.400	29.120	27.714	27.462	28.000	29.030	29.208	28.940	29.300	30.210
2	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000	0.000
3	21.129	23.603	23.700	24.100	19.469	22.067	23.050	23.800	26.595	22.455	25.700	25.100
4	10.465	11.910	11.980	11.980	10.251	9.714	11.020	10.900	10.713	14.277	12.980	12.880
5	12.478	13.561	14.010	15.200	10.542	9.930	12.110	14.200	15.267	17.121	15.010	16.200
6	5002.097	4670.525	4623.525	5070.525	3484.312	3058.983	4521.550	4172.250	6049.616	7613.624	4613.250	4970.520
7	31.194	26.965	29.021	31.230	21.188	19.381	28.210	27.230	46.530	34.350	30.210	32.230
8	0.008	0.009	0.009	0.009	0.006	0.007	0.008	0.008	0.010	0.010	0.009	0.009
9	7.263	8.014	8.110	8.120	4.281	4.576	6.410	7.820	10.615	11.841	8.210	8.420
10	55 783	56 770	57 100	57.020	36 114	50.140	56 200	55 120	58 648	74 210	67 100	57 020

TABLE XI

MEAN, BEST, AND WORST OBTAINED FITNESS COMPUTED FOR ANN WEIGHTS ADAPTATION ON REGRESSION PROBLEMS

TABLE XII Average Std, RMSE, and Run Time Computed for the Data Regression Data Sets

	Standard dev.					RMSE				Run time			
Data No.	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	EGWO	GWO	PSO	GA	
1	0.831	0.777	0.759	0.071	28.364	28.825	28.041	27.976	521.445	512.704	511.659	511.299	
2	0.000	0.000	0.000	0.000	0.000	0.000	1.395	0.353	560.938	555.138	560.240	559.460	
3	2.591	1.521	1.636	3.519	22.862	21.395	22.535	21.425	563.576	557.476	554.709	554.533	
4	0.233	2.286	2.518	3.089	11.294	11.261	13.751	11.289	493.753	492.448	492.383	490.624	
5	2.475	3.596	5.072	4.644	12.502	13.347	12.774	13.811	516.478	510.807	511.708	511.149	
6	1345.756	2552.641	2549.730	2555.025	7046.083	9339.405	9341.492	9339.002	518.771	511.579	516.759	509.278	
7	13.486	7.486	7.534	8.673	41.986	42.833	42.906	43.061	518.126	512.300	511.748	514.316	
8	0.002	0.002	0.047	0.040	0.008	0.008	0.007	0.008	0.008	0.009	0.009	0.009	
9	3.183	3.648	3.066	5.619	40.595	36.636	36.554	37.956	522.074	515.252	519.330	512.944	
10	4.888	23.743	24.597	22.829	78.676	69.748	69.588	70.035	504.27	516.118	512.634	511.532	

B. Multilayer ANNs Weight Adaptation

Feed-forward multilayer ANNs have been widely used as nonlinear function approximator that maps a given input to a given output. Commonly, the mapping function is either classification function, when the output is in discrete form, or regression when the output is in continuous form. The primary challenge is to estimate the weight set for such a network in order to achieve a proper mapping. Back propagation is commonly used to train the weights but, since it is gradientbased, it suffers from convergence to local optima [29]. Recently, other algorithms were employed for such tasks, such as GA [30] or PSO [31]. A generic representation of such models selects a weight set that minimizes the total error over all training data

min
$$E(W) = \frac{1}{q * O} \sum_{k=1}^{q} \sum_{i=1}^{O} \left(y_i^k - C_i^k \right)^2$$
 (34)

where q is the number of training samples, O is the number of nodes in the output layer, y_i^k and C_i^k are the actual and the desired output of the training point k on the output node i, and W is the vector of all neural network weights and biases. The weight range is usually set to [0, 1] or [-1, 1] [29]. The error function is used as a fitness function in the optimization problem of selecting appropriate weights that minimize the error between the predicted and the actual output. The network structure was assumed to be static and the challenge is to select the weight set in the range [-1, 1].

GWO has been successfully applied to train the multilayer ANNs for classification and regression problems [32]. In the tests performed in [32], GWO dominates all the other methods used for comparison (GA, PSO, ant colony optimization, evolution strategies, and population-based incremental learning) for the regression tests and is only dominated by the GA for three of the classification tests. This motivates this paper to try to get even better results with our improved EGWO. In this paper, a two-layered feed-forward ANN is used for regression problems. Ten data sets given in Table X are used for experiments. Each individual data set is divided following a k-fold cross validation manner, with k=10 and the experiments repeated 30 times. In the k-fold cross validation, kth fold is used as testing data and the remaining data are employed for training.

1) Results and Discussion: Table XI presents the results of the statistical measures for all the data sets. We can observe that the EGWO has better fitness function value, which proves the capability of the model to converge to better optima. The enhanced performance can be interpreted by the fact that the EGWO can exploit agents' own experience to adapt the exploration rate per search agent. The exploration rate control helps the optimizer to quickly jump to more promising regions especially in complex search space. The results in Table XII show that both GWO and EGWO have comparable std, which ensures the repeatability of results regardless of the random factors used. From the performance on the test data, we can observe that EGWO has a better performance than GWO. The small difference in the running time is because EGWO employs a more complex methodology, but even so, the difference is not really sensitive.

V. CONCLUSION AND FUTURE WORK

In this paper, a variant of GWO that learns the exploration rate in an individual manner for each agent (wolf) is proposed. The experienced GWO (EGWO) uses reinforcement learning principles to learn the actions that should be taken at different states of the optimization and in various regions of the search space. A neural network model was used to hold the experience information. The proposed EGWO is compared with the original GWO, PSO, and GA on two main optimization applications: feature selection and ANN weight adaptation. Results were assessed in both applications using a set of performance indicators. We observe a significant improvement in the performance of EGWO while compared with the other methods. EGWO can adapt quickly to different search space terrains and can avoid premature convergence. Besides, the initialization of the search agents positions at the beginning of the optimization process plays a role in the performance of EGWO, with uniform and MRMR initialization providing more variability in the search agents, helping the experienced model to be easily trained. Our methodology is more of a proof of concept that an automatic rather than manual (via trial and error) setting of the parameters of learning algorithms is more efficient, and can be generalized to other similar algorithms, thus helping with the tedious task of always finding the right parameter configuration for a particular application.

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